

The Crystal Structure of Magnesium Thiosulphate Hexahydrate

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Magnesium thiosulphate hexahydrate, $\text{Mg}(\text{OH}_2)_6\text{S}_2\text{O}_3$, crystallizes in the space group $D_{3h}^{15}-Pnma$, with unit-cell dimensions $a = 9.32$, $b = 14.36$, $c = 6.87$ Å, and with $Z = 4$. The structure consists of alternating layers of $\text{Mg}(\text{OH}_2)_6^{2+}$ octahedra and $\text{S}_2\text{O}_3^{2-}$ tetrahedra perpendicular to the b axis. Each octahedron is linked by $\text{OH} \cdots \text{O}$ hydrogen bonding to four surrounding octahedra in the same layer and to four tetrahedra in the two adjacent layers. An $\text{OH} \cdots \text{S}$ type of interaction, probably due to hydrogen bonding, is observed.

Introduction

An X-ray study of magnesium thiosulphate hexahydrate, $\text{Mg}(\text{OH}_2)_6\text{S}_2\text{O}_3$, was carried out by Brunt (1946), but the proposed model was not consistent with the tetrahedral structure of the $\text{S}_2\text{O}_3^{2-}$ ion.

A new determination of the structure is reported in the present paper. The results are consistent with those found by Taylor & Beevers (1952) in $\text{Na}_2\text{S}_2\text{O}_3 \cdot 5\text{H}_2\text{O}$, by Sándor & Csordás (1960) in $\text{Na}_2\text{S}_2\text{O}_3$, and by us in $\text{BaS}_2\text{O}_3 \cdot \text{H}_2\text{O}$ (to be published).

Experimental

$\text{Mg}(\text{OH}_2)_6\text{S}_2\text{O}_3$ crystallizes in colourless flat prisms. As the crystals are hygroscopic, the one used for X-ray analysis was sealed in a Lindemann tube.

The crystal data, deduced from rotation and Weissenberg photographs ($\text{Cu } K\alpha$) around the elongation axis $[001]$, agree with those reported by Brunt and with the axial ratio found by Fock & Klüss (1891):

$$a = 9.32 \pm 0.01, \quad b = 14.36 \pm 0.04, \quad c = 6.87 \pm 0.01 \text{ \AA}, \\ V = 919 \text{ \AA}^3, \quad Z = 4, \quad D_c = 1.766, \quad D_o = 1.818 \text{ g.cm.}^{-3}$$

(Oliver, reported in Groth, 1909), $\mu = 62.2 \text{ cm.}^{-1}$, $F(000) = 512$.

Space group (from systematic absences): $D_{2h}^{16}-Pnma$ or $C_{2v}^9-Pn2_1a$.

The intensity data were obtained photometrically from $hk0$, $hk1$ and $hk2$ multiple-film, Weissenberg photographs. $62hk0$ (possible 87), $103hk1$ (possible 174) and $115hk2$ (possible 168) independent reflections were observed.

Corrections for absorption were calculated assuming a cylindrical sample of mean radius 0.03 cm. A preliminary scale factor was obtained by Wilson's method.

Structure determination and refinement

To solve the phase problem, the coincidences method of Grant, Howells & Rogers (1957) was applied to the

$hk0$ reflections adopting, as a starting hypothesis, the space group $Pnma$. Using the 29 reflections with $0.20 \leq U \leq 0.51$, a rough Fourier projection was calculated. The successive results showed that the space group and the signs were correct, except for three weak reflections.

The first value of $R(hk0)$, 0.243, indicated a correct interpretation of the Fourier projection. A new electron-density projection was then evaluated to improve the x and y coordinates.

An initial set of z coordinates was derived by considering the packing of the ionic polyhedra and assuming for $\text{S}_2\text{O}_3^{2-}$ the dimensions found in $\text{Na}_2\text{S}_2\text{O}_3 \cdot 5\text{H}_2\text{O}$ by Taylor & Beevers. These coordinates gave the following R values:

$$R(hk0) = 0.223, \quad R(hk1) = 0.192, \quad R(hk2) = 0.175.$$

In Fig. 1 the final projection $\rho_0(X, Y)$ is shown.

Three cycles of Booth's differential synthesis were carried out, the atomic coordinates and the isotropic thermal parameters being determined from the observed and calculated values of the electron densities and from their first and second derivatives. Anisotropic

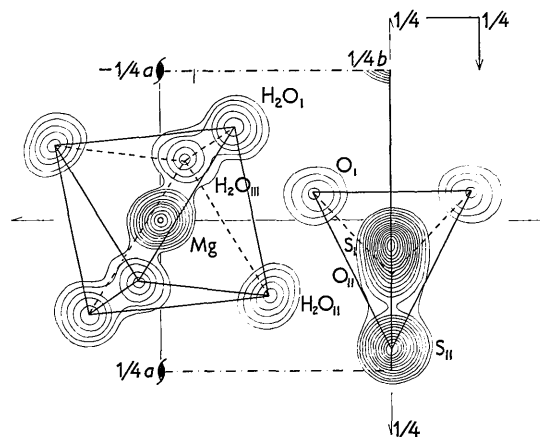


Fig. 1. Electron-density projection $\rho_0(X, Y)$. Contour interval 2 e. \AA^{-2} , first line at 4 e. \AA^{-2} .

Table 3. Comparison of peak heights and curvatures from differential synthesis

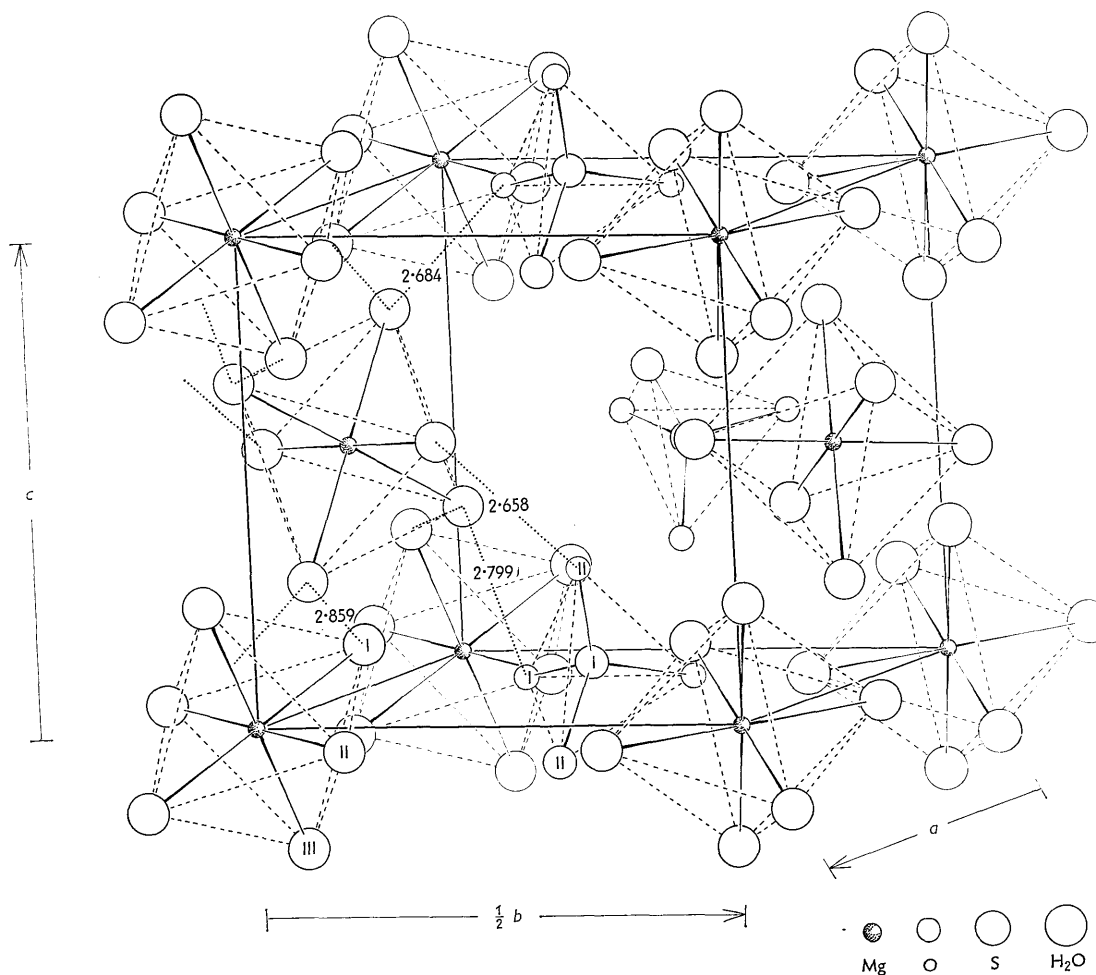
	ρ (e.Å ⁻³)		$-A_{hh}$ (e.Å ⁻⁵)		$-A_{kk}$ (e.Å ⁻⁵)		$-A_{ll}$ (e.Å ⁻⁵)	
	obs.	calc.	obs.	calc.	obs.	calc.	obs.	calc.
Mg	15.3	15.9	196.7	187.9	175.2	175.6	24.2	24.6
S _I	19.8	20.3	229.8	224.5	239.5	232.0	29.5	29.5
S _{II}	19.1	19.5	234.0	224.2	206.7	202.9	30.8	30.8
O _I	6.4	6.8	61.9	62.2	48.3	42.0	9.9	10.0
O _{II}	6.4	6.8	45.8	46.3	64.5	55.6	6.1	6.5
H ₂ O _I	8.8	8.3	94.7	81.0	92.2	85.4	13.9	13.1
H ₂ O _{II}	8.0	8.0	92.1	89.2	78.7	78.7	12.2	12.4
H ₂ O _{III}	7.5	7.7	64.0	63.8	71.9	72.5	11.7	12.3

$$R(hk0)=0.117, R(hk1)=0.102, R(hk2)=0.116.$$

F_o and F_c are listed in Table I, where F_c is calculated from the final atomic coordinates and thermal parameters in Table 2. The atomic scattering factors used were those of Berghuis *et al.* (1955) for O and Mg²⁺, and those of Dawson (1960) for S.

The standard deviations of atomic coordinates and thermal parameters have been estimated by the

method of Cruickshank (1949, 1956) for observed reflections only. The largest values are for the $\sigma(z)$'s, owing to the small number of reciprocal lattice layers considered. This is also responsible for the particularly small values of $A_{ll}=(\partial^2\rho/\partial z^2)_{r=0}$; but the agreement between the observed and calculated values for the electron densities and their second derivatives at the atomic peaks is good (Table 3). The standard deviation of the electron density is $\sigma(\rho)=0.206$ e.Å⁻³.

Fig. 2. Clinographic projection of the structure of Mg(OH₂)₆S₂O₃.

Discussion

Fig. 2 is a clinographic projection of one half of the unit cell. Each Mg atom is surrounded by six water molecules arranged at the corners of a nearly regular octahedron, as the following values of bond distances and angles indicate:

Mg-H ₂ O _I	2.115 ± 0.011 Å
Mg-H ₂ O _{II}	2.068 ± 0.008
Mg-H ₂ O _{III}	2.068 ± 0.020
H ₂ O _I -Mg-H ₂ O _{II}	89.1 ± 0.4°
H ₂ O _I -Mg-H ₂ O _{III}	90.5 ± 0.6
H ₂ O _{II} -Mg-H ₂ O _{III}	90.5 ± 0.6

The standard deviations are calculated from the formulae of Ahmed & Cruickshank (1953) for bond lengths and by Darlow (1960) for angles.

The distances Mg-OH₂ agree well with those already found for Mg(OH₂)₆²⁺; e.g. 2.04 Å (mean value) in magnesium benzene sulphonate hexahydrate (Broomhead & Nicol, 1948), 2.08 and 2.12 Å in magnesium phosphite hexahydrate (Corbridge, 1956).

The distances and angles in the tetrahedral thio-sulphate group are in good agreement with those found in sodium thiosulphate pentahydrate by Taylor & Beevers (1952) and in anhydrous sodium thiosulphate by Sándor & Csordás (1960):

	Present study	Taylor & Beevers	Sándor & Csordás
S _I -S _{II}	2.020 ± 0.008 Å	1.97 Å	2.01 Å
S _I -O _I	1.484 ± 0.014	1.46	1.46 ± 0.05
S _I -O _{II}	1.479 ± 0.040	1.59	
		1.40	
O _I -S _I -O _I '	110.9 ± 1.1°	104-115°	110.5 ± 1.5°
O _I -S _I -O _{II}	111.0 ± 1.1		
O _I -S _I -S _{II}	107.6 ± 0.8		
O _{II} -S _I -S _{II}	108.5 ± 0.8		

The other interatomic distances shorter than 3.5 Å are as follows. (When the coordinates are not indicated the atom is at *x, y, z*.)

H ₂ O _I -O _I	2.799 ± 0.027 Å
H ₂ O _I -O _{II}	3.387 ± 0.015
H ₂ O _I -O _{III} ($x - \frac{1}{2}, y, \frac{1}{2} - z$)	3.470 ± 0.016
H ₂ O _I -S _{II} ($x - \frac{1}{2}, y, \frac{1}{2} - z$)	3.246 ± 0.013
H ₂ O _I -H ₂ O _{III} ($-\frac{1}{2} - x, y, \frac{1}{2} + z$)	2.859 ± 0.014
H ₂ O _{II} -O _{II}	2.658 ± 0.032
H ₂ O _{II} -O _I ($\frac{1}{2} + x, y, \frac{1}{2} - z$)	3.172 ± 0.014
H ₂ O _{II} -S _{II} ($x, y, z - 1$)	3.195 ± 0.018
H ₂ O _{II} -H ₂ O _I ($\frac{1}{2} + x, y, \frac{1}{2} - z$)	3.371 ± 0.023
H ₂ O _{II} -H ₂ O _{III} ($\frac{1}{2} + x, y, -\frac{1}{2} - z$)	3.199 ± 0.018
H ₂ O _{III} -O _I ($x, y, z - 1$)	2.684 ± 0.024

The distances shorter than 3 Å are probably hydrogen bonds. The packing of the octahedral cations and the tetrahedral anions is determined by these interactions. The structure as a whole is built up from alternating layers of octahedra and tetrahedra; the layers are parallel to (010) and succeed each other at intervals of $\frac{1}{4}b$. Each octahedron is bonded to the four surrounding octahedra in the same layer by a hydrogen bond (2.86 Å) and with six hydrogen bonds directed towards the oxygens in the adjacent layers of tetrahedra. These hydrogen bonds are stronger than the previous ones within the layers, as indicated by the shorter distances (2.66, 2.68, 2.80 Å).

The experimental data are insufficient to determine the distribution of H atoms. Nevertheless, a plausible guess for this distribution can be made by considering an idealized tetrahedral model of the H's and lone pairs in the water molecule. Assuming one lone pair directed towards Mg²⁺, the H's will probably orientate towards those atoms which are in the best condition for hydrogen bonding. The environments for H₂O_I, H₂O_{II} and H₂O_{III} are shown in Fig. 3(a), (b) and (c) respectively. In these figures probable orientations of H's and lone pairs are also indicated. The lone pairs have been directed in the first case (Fig. 3(a)) towards a water molecule behaving as a proton donor, in the others towards an oxygen atom (Fig. 3(b)) and a water molecule (Fig. 3(c)) which are rather distant

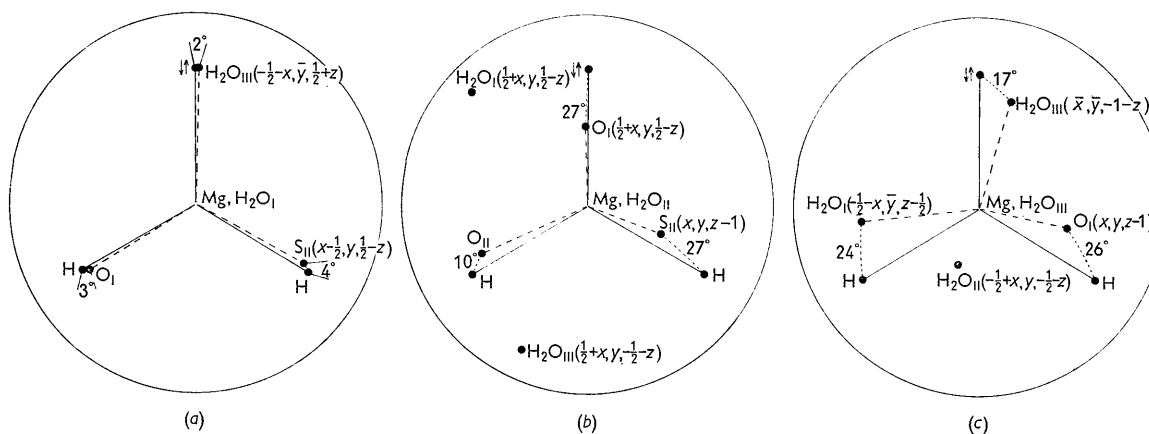


Fig. 3. Stereographic projection of the environment of (a) H₂O_I, (b) H₂O_{II}, (c) H₂O_{III} viewed down the H₂O-Mg bonds. The orientation of H's and lone pairs (↓↑) is hypothetical.

(3.17 and 3.81 Å respectively). The hydrogen bonding $\text{H}_2\text{O}_{\text{I}} \cdots \text{S}_{\text{II}}$ satisfies particularly well the angular criterion of Donohue (1952) but the same cannot be said for $\text{H}_2\text{O}_{\text{II}} \cdots \text{S}_{\text{II}}$.

The calculations at the refinement stage were performed on the IBM 650 computer of the *Centro Calcoli e Servomeccanismi della Università di Bologna* using the programmes of L. H. Jensen for the structure factors calculations and those of R. Shiono for the differential synthesis. The cost of the computing work was borne by the *Consiglio Nazionale delle Ricerche*. It is a pleasure to thank all these people and Prof. L. Cavalca for his valuable interest.

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The Structures of Substituted Triazolopyrimidines. Part I. 2-Amino 5-propyl 7-methyl s-triazolo [2,3-c] Pyrimidine Hydrochloride

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The molecular structure of $\text{C}_9\text{H}_{13}\text{N}_5 \cdot \text{HCl}$, a biologically active triazolo-pyrimidine, has been determined by X-ray methods. The crystals are monoclinic, with the unit-cell parameters

$$a = 22.30 \pm 0.07, \quad b = 6.41 \pm 0.02, \quad c = 16.76 \pm 0.05 \text{ \AA}, \quad \beta = 107.7 \pm 0.5^\circ.$$

There are eight molecules in the unit cell, and the space-group is $C2/c$. The three-dimensional Patterson synthesis confirmed this space group, and excluded the alternative, Cc . The structure was solved by the use of Buerger's minimum function, which was derived graphically from the Patterson synthesis. Refinement by Fourier and least-squares methods was continued until the final average standard deviation of the atomic positions was 0.017 Å.

The substance was shown to be a triazolo [2,3-c] pyrimidine, with the structure I. The two fused rings are planar and inclined at 6° to each other. The bonds in the fused ring system are all shorter than normal single-bonds, but simple resonance theory is not adequate to explain them. The molecules are linked by a spiral chain of hydrogen bonds 3.18 and 3.30 Å long between the chloride ion and the primary amine group N10; there are also other inter-ionic contacts less than 3.5 Å long which cannot all be hydrogen bonds.

Introduction

In the course of work on a variety of substituted triazolopyrimidines which have interesting biological properties, a substance with the empirical formula $\text{C}_9\text{H}_{13}\text{N}_5$ was isolated, and was thought to be the triazolo [2,3-c] pyrimidine, I, or the [4,3-c] isomer, II, (Davies, Miller & Rose 1960; Miller & Rose 1960). The chemical and spectroscopic evidence was not

conclusive however, and the X-ray analysis described in this paper was therefore undertaken.

